

### 3 同次形 Homogenous equations

#### 3.1 p.17

Consider the following differential equation,

$$xy \frac{dy}{dx} = x^2 + y^2. \quad (*)$$

- (a) Find the general solution of (\*).
- (b) Eliminate an arbitrary constant in the solution obtained in (a) and verify whether (\*) can be derived.
- (c) Verify whether the solution derived in (a) satisfies the equation (\*).

#### 3.2 p.12, 14,17

Find the general solution for each of the following differential equations;

- (1)  $3xy^2y' = x^3 + y^3$
- (2)  $(x^2 + xy)y' = y^2$

#### 3.3

Find the particular solution for the following differential equation

$$xy' = y + x \cot(y/x)$$

that satisfies the initial condition  $y = 0$  at  $x = \sqrt{2}$ .